

# Student #1

D#

Section #

A

## Problem 3

To raise money for a University scholarship fund, the new IT dean has volunteered to bungee jump from a crane if contributions can be found for 10 scholarships. To add some interest, the jump will be made from 42m above a pool of water. A 30m bungee cord would be attached to the dean. First you must convince the dean that your plan is safe for a person of his mass, 70kg. The dean knows that as the bungee cord begins to stretch, it will exert a force which has the same properties as the force exerted by a spring. Your plan has the dean stepping off a platform and being in free fall for 30m before the cord begins to stretch.

- (a) Determine the spring constant of the bungee cord so that it stretches only 12m, which will just keep the dean out of the water. (Assume that the dean is a point-like object).
- (b) Using the result of (a), find the dean's speed 7m above the water.



apply second law:

$$F = ma = RX - mg$$

Because the system has no acceleration at the bottom of the jump:

$$0 = RX - mg$$

$$mg = RX$$

$$R = \frac{mg}{x} = 52.225 \text{ N/m}$$

$$\boxed{\text{(a) } 52.225 \text{ N/m}}$$

$$mgh_1 = \frac{1}{2}kd^2 = \frac{1}{2}k(d-7)^2 + mgh_2 + \frac{1}{2}mv^2$$

$$mgh_1 = \frac{1}{2}k \cdot 25 + mgh_2 + \frac{1}{2}mv^2$$

$$2mg(h_1 - h_2) = 25k + mv^2$$

$$\frac{2mg(h_1 - h_2) - 25k}{m} = v^2$$

$$v = \sqrt{\frac{2mg(h_1 - h_2) - 25k}{m}}$$

$$\boxed{\text{(b) } v = 25.847 \text{ m/s}}$$

$$\begin{aligned} h_1 &= 42\text{m} \\ h_2 &= 7\text{m} \\ d &= 12\text{m} \end{aligned}$$

# Student #2

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Section #

A

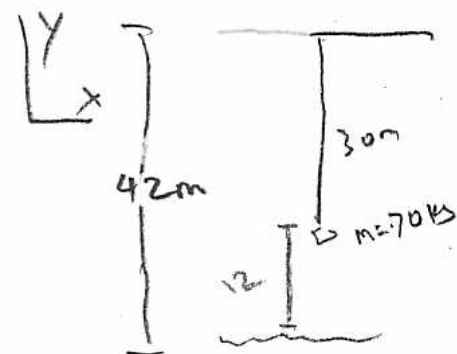
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(b) Using the result of (a), find the dean's speed 7m above the water.

(a)



$k?$  12m

$$k = \frac{\sqrt{2(70)(9.8)(12) + 70(24.25)^2}}{12}$$

$$k = 20 \text{ N/m}$$

$V_f$  at 30m

$$V_f^2 = V_0^2 + 2ax$$

$$V_f^2 = 0 + 2(9.8)(30)$$

$$V_f = \sqrt{588} = 24.25 \text{ m/s}$$

cons. of energy

$$mgh + \frac{1}{2}mv^2 = \frac{1}{2}kx^2$$

$$\sqrt{kx^2} = \sqrt{2mgh + mv_i^2}$$

$$kx = \frac{\sqrt{2mgh + mv_i^2}}{x}$$

$$k = \frac{\sqrt{2mgh + mv_i^2}}{x}$$

(b)

cons of energy

$$mgh = \frac{1}{2}mv_f^2 + \frac{1}{2}kx^2$$

$$mgh - \frac{1}{2}kx^2 = \frac{1}{2}mv_f^2$$

$$\sqrt{\frac{2mgh - kx^2}{m}} = v_f$$

$$v_f = \sqrt{\frac{2(70)(9.8)(42) - (20)(35)^2}{70}}$$

$$v_f = 21.75 \text{ m/s}$$

# Student #3

A

Section #

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$$F_T = kx$$

$$F_T = F_g$$

$$F_{g \text{ Dean}} = mg$$

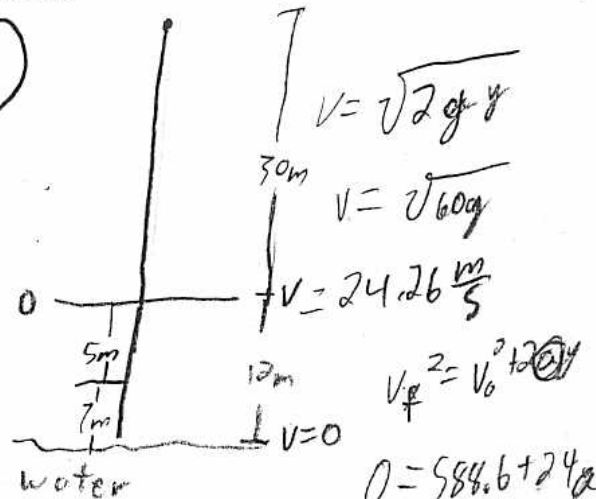
$$kx = mg$$

$$k(12) = 70g$$

$$k = \frac{70g}{12m}$$

$$d) \quad k = 57.23 \frac{N}{m}$$

b)



$$0 = 588.6 + 24a$$

$$a = -24.5 \frac{m}{s^2}$$

$$v_f^2 = 588.6 - 245.25$$

$$v_f = 18.53 \frac{m}{s}$$

7m above the water

# Student #4

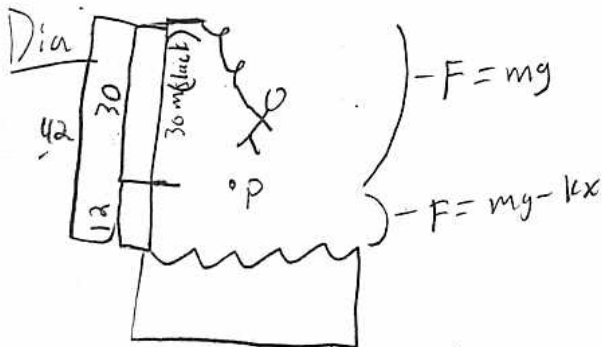
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Physics:  
energy

Variables:

$$h_{\text{tot}} = 42$$

$$D = 7$$

$$m = 70$$

Equ<sup>n</sup>:

$$U_{\text{pot}} = Mgh$$

$$U_{\text{kin}} = \frac{1}{2}mv^2$$

$$U_{\text{spring}} = \frac{1}{2}kx^2$$

manipulate:

$$U_{\text{sys}} = Mgh$$

@ water surface

$$Mgh = \frac{1}{2}kx^2$$

$$k = \frac{2Mgh}{x^2}$$

$$k = \frac{2(70)(9.8)(42)}{(12)^2}$$

$$k = 400$$

Part B: Potential = spring + kinetic + potential

$$Mgh = \left(\frac{1}{2}kx^2\right) + \left(\frac{1}{2}mv^2\right) + (mgd)$$

$$\frac{1}{2}mv^2 = Mgh - \frac{1}{2}kx^2 - mgd$$

$$v = \sqrt{\frac{2(Mgh - \frac{1}{2}kx^2 - mgd)}{m}}$$

$$v = \sqrt{\frac{2(70 \cdot 9.8 \cdot 42 - \frac{1}{2}(400)5^2 - 70 \cdot 9.8 \cdot 7)}{70}}$$

$$v = 23.31 \frac{\text{m}}{\text{s}}$$

analysis:

this answer is reasonable seeing as his velocity @ point P was 24.25

# Student # 5

D#

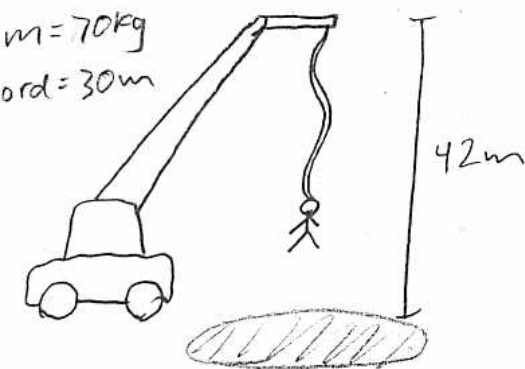
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- (b) Using the result of (a), find the dean's speed 7m above the water.



$$F = -kx$$

$$a) \quad ma = -kx$$
$$(70\text{kg})(9.8\text{m/s}^2) = k(12\text{m})$$

$$k = \frac{ma}{x} = \boxed{57.2 \text{ N/m}}$$

$$b) \quad v^2 = v_0^2 + 2a(\Delta x)$$

$$v_0 = \sqrt{mgh} \quad (\text{where } h = 30\text{m})$$

$$\Delta x = 5\text{m}$$

$$a = \frac{-\sqrt{mgh}}{12\text{m}}$$

$$v = \sqrt{\sqrt{mgh} + 2\left(\frac{-\sqrt{mgh}}{12\text{m}}\right)(5)}$$

$$v = \sqrt{143 + 2(-12)(5)} = \boxed{16\text{m/s}}$$

# Student #6

A

D#

Section #

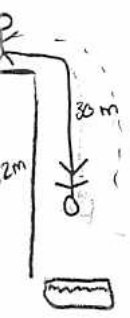
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$$k = \frac{F}{x}$$

(b) Using the result of (a), find the dean's speed 7m above the water.



a.  $x = 12 \text{ m}$ ,  $F = ma$ ,  $a = -9.8 \text{ m/s}^2$

$$F = -kx$$

$$ma = -kx$$

$$(70 \text{ kg})(-9.8 \text{ m/s}^2) = -k(12 \text{ m})$$

$$k = 57.167 \frac{\text{N}}{\text{m}}$$

b. Use conservation of Energy

$$PE_{\text{top}} = KE_{\text{bottom}} + PE_{\text{bottom}}$$

$$mgh = \frac{1}{2}mv^2 + \frac{1}{2}kx^2$$

$\therefore x$  equals  $12 \text{ m} - 7 \text{ m} = 5 \text{ m}$  because that is the distance the spring will be stretched

\* The dean will have PE at the top of his jump and then KE and PE at the bottom because the bungee will shoot him back

$$(70 \text{ kg})(57.167)(42 \text{ m}) = \frac{1}{2}(70 \text{ kg})(v^2) + \frac{1}{2}(57.167)(5 \text{ m})^2$$

$$v^2 = \frac{(70 \text{ kg})(57.167)(42) - \frac{1}{2}(57.167)(5)^2}{\frac{1}{2}(70 \text{ kg})}$$

$$v = 69.15 \text{ m/s}$$



# Student # 7

ID#

Section #

A

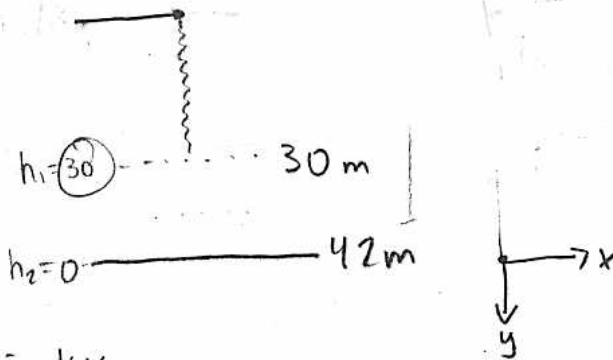
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(b) Using the result of (a), find the dean's speed 7m above the water.

Know  
 $h = 42\text{ m}$   
Cord = 30 m  
 $m = 70\text{ kg}$



Want  
"k" so  $x = 12\text{ m}$

$$a) F_{\text{spring}} = -kx$$

$$E_{\text{spring}} = \frac{1}{2}kx^2$$

$$E_i = E_f$$

$$E_i = mgh_i + \frac{1}{2}kx^2$$

$$E_f = mgh_f + \frac{1}{2}kx^2$$

$$mgh_i + \frac{1}{2}kx^2 = \frac{1}{2}kx^2$$

$$mgh_i = \frac{1}{2}kx^2$$

$$k = \frac{mgh_i}{\frac{1}{2}x^2} \Rightarrow k = \frac{(70)(9.8)(30)}{\frac{1}{2}(12)^2} \Rightarrow k = 285.8$$

b) 7m above water  $\Rightarrow x = 5$

$$w = \sqrt{\frac{k}{m}} \quad w = \sqrt{\frac{285.8}{70}} = 2 \text{ rad/sec}$$

# Student #8

ID#

Section #

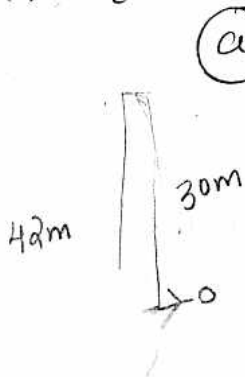
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(b) Using the result of (a), find the dean's speed 7m above the water.



(a)

Given!

$$D = 42 \text{ m}$$

$$l = 30 \text{ m}$$

$$m = 70 \text{ kg}$$

Force exerted by spring

$$F = k\Delta x$$

in this case:  $F = k \Delta y = 32.6 \frac{\text{N}}{\text{m}} \times 42 \text{ m} = 1369 \text{ N}$

Conservation of energy

$$KE + PE = E$$

$$PE_{\text{rope}} + KE_i + PE_i = KE_f + PE_f$$

$$\frac{1}{2} kx^2 + 0 - mgh = \frac{1}{2} mv^2 + mgh$$

$$\frac{1}{2} kx^2 = mgh$$

$$k = \frac{2mgh}{x^2} = \frac{2 \times 70 \text{ kg} \times 9.8 \text{ m/s}^2 \times 42 \text{ m}}{(42 \text{ m})^2} = 32.6 \text{ N/m}$$

(b)

bungee rope length = 30m

total length = 42m

$$42 \text{ m} - 7 \text{ m} = 35 \text{ m}$$

$$KE + PE = KE + PE$$

$$\frac{1}{2} mv^2 + 0 = 0 + \frac{1}{2} kx^2$$

$$v^2 = \frac{kx^2}{m}$$

$$v = \sqrt{\frac{kx^2}{m}} = \frac{32.6 \frac{\text{N}}{\text{m}} (35 \text{ m})^2}{70 \text{ kg}} = 24.0 \text{ m/s}$$



# Student #9

ID#

Section #

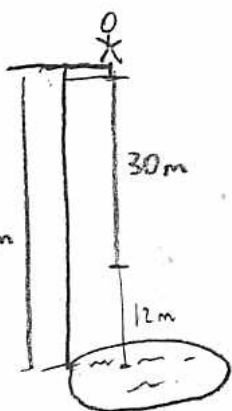
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(b) Using the result of (a), find the dean's speed 7m above the water.



$$\text{mass} = 70\text{kg}$$

find  $k$ ?

$$F = k\Delta x \quad \Delta x = 12\text{m}$$

$F =$  that of him falling 30m

$$F = mg = (70)(9.8) = 686\text{ N}$$

$$k = \frac{F}{\Delta x} = \frac{686}{12} = \boxed{57.16\text{ N/m}}$$

$x = 12 - 7 = 5$

$$\frac{1}{2}mv^2 + mgh = mgh$$

$$mgh = \frac{1}{2}kx^2 + \frac{1}{2}mv^2 + mgh$$

$$(70)(9.8)(42) = \frac{1}{2}(57.16)(5)^2 + \frac{1}{2}70v^2 + (70)(9.8)(7)$$

$$28812 = 714.5 + 35v^2 + 4802$$

$$\frac{35v^2}{35} = \frac{23295.5}{35}$$

$$v^2 = 665.58$$

$$\boxed{v = 25.8\text{ m/s}}$$

# Student #10

A

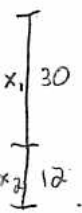
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(b) Using the result of (a), find the dean's speed 7m above the water.



a) Conservation of Energy  
 $PE = KE \Rightarrow mgh = \frac{1}{2}mv^2$   
 $gh = \frac{1}{2}v^2$

$$\sqrt{2gh} = v$$
$$\sqrt{2(9.8)30} = v$$
$$24.25 = v$$

$$KE = SE$$
$$\frac{1}{2}mv^2 = \frac{Kx^2}{2}$$
$$\frac{mv^2}{x^2} = K$$
$$K = \frac{(70)(24.25)^2}{(12)^2}$$

$$K = 285.86$$

$$SE = \frac{Kx^2}{2}$$

b)  $\int_5^{30}$   $KE = SE = PE ?$

$$\frac{1}{2}mv^2 = \frac{Kx^2}{2}$$
$$v^2 = \frac{Kx^2}{m}$$
$$v = \sqrt{\frac{Kx^2}{m}}$$
$$v = \sqrt{\frac{(285.86)(5)^2}{70}}$$

$v = 10.1 \text{ m/s}$  at 7m above water

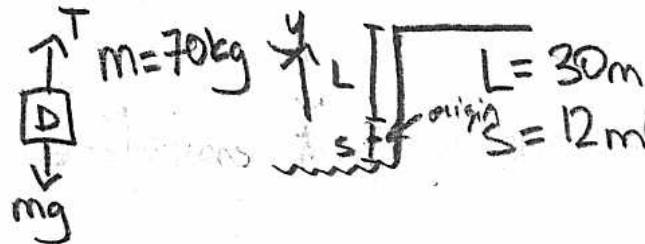
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$$\begin{aligned}
 x &= A \cos(\omega t) & \omega &= \sqrt{k/m} \\
 v &= -A \omega \sin(\omega t) \\
 a &= -A \omega^2 \cos(\omega t)
 \end{aligned}$$



~~equilibrium at  $mg = kx$~~

$$v_i^2 = 0 - 2Lg \quad v_i = -\sqrt{2Lg} = v_{\max}$$

$$v_{\max} = -A\omega \Rightarrow \sqrt{2Lg} = A\sqrt{k/m} \Rightarrow 2Lg = \frac{A^2 k}{m}$$

$$x_{\max} = \frac{s}{2} \Rightarrow \frac{s}{2} = A \Rightarrow A^2 = \frac{s^2}{4} \Rightarrow 2Lg = \frac{s^2 k}{4m}$$

$$k = \frac{8Lgm}{s^2} \Rightarrow \frac{8(30m)(9.8m/s^2)(70kg)}{(12m)^2} = \boxed{1100N/m}$$

$$x = A \cos(\omega t) \quad A = \frac{s}{2}, \quad \omega = \sqrt{k/m} \Rightarrow x = \frac{s}{2} \cos(\omega t)$$

$$1m = \frac{2m}{2} \cos\left(\sqrt{\frac{1100N/m}{70kg}} t\right) \quad t = 0.35s \quad x = 7m - 12m + 6m = 1m$$

$$v = \sqrt{2Lg} \sin\left(\sqrt{k/m} t\right) = \sqrt{2 \times 30m \times 9.8m/s^2} \sin\left(\sqrt{\frac{1100N/m}{70kg}} \times 0.35\right) = \boxed{24m/s}$$

# Student # 12

A

ID#

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- (b) Using the result of (a), find the dean's speed 7m above the water.

$$E = \frac{1}{2}mv^2 + mgh + \frac{1}{2}kx^2$$

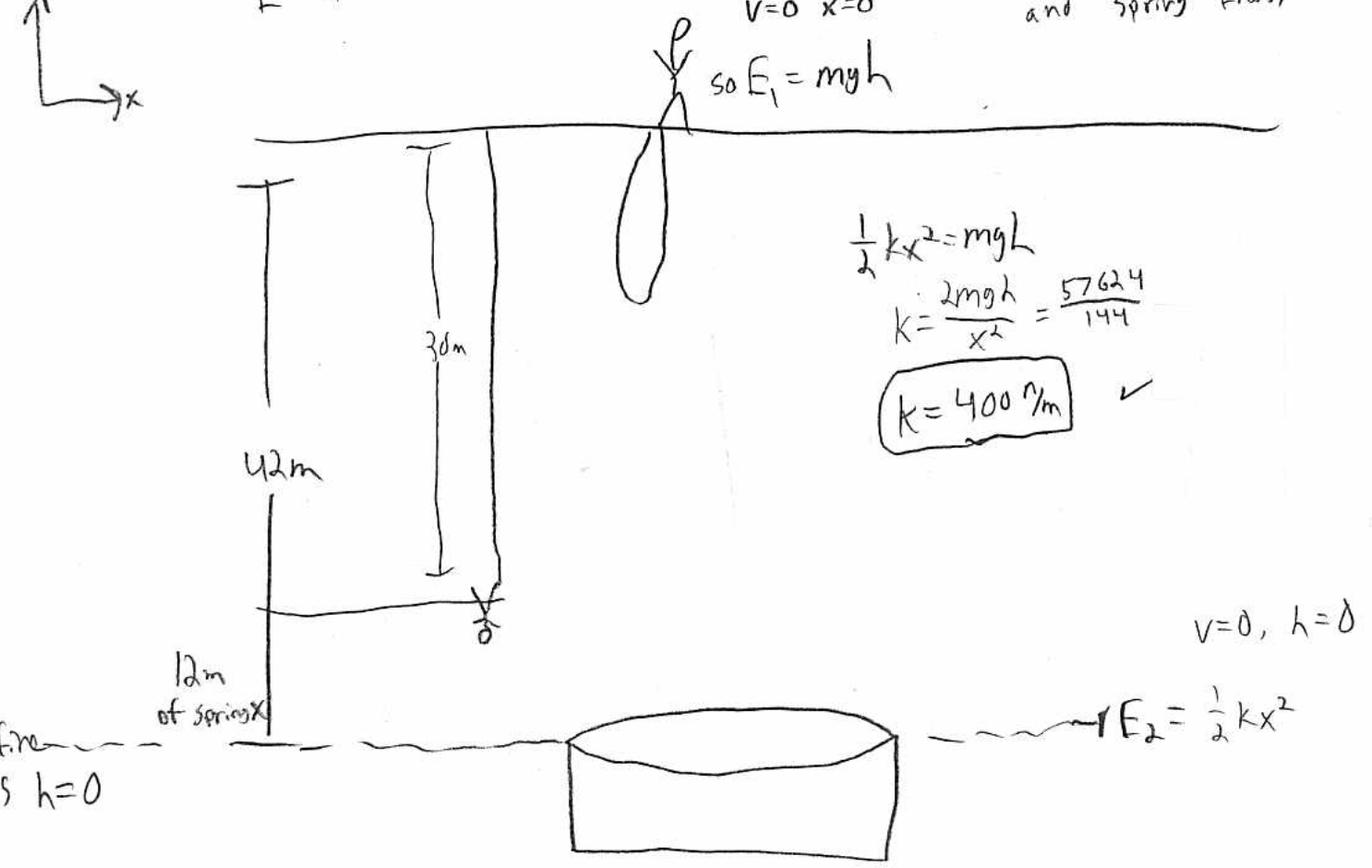
Use conservation of PE, KE and Spring Energy

$v=0, x=0$   
so  $E_1 = mgh$

$$\frac{1}{2}kx^2 = mgh$$

$$k = \frac{2mgh}{x^2} = \frac{57624}{144}$$

$$k = 400 \text{ N/m}$$



$v=0, h=0$

$E_2 = \frac{1}{2}kx^2$

at the water surface  $h=0$

Speed 7m above H<sub>2</sub>O:

$$\frac{1}{2}mv^2 + \frac{1}{2}kx^2 = E$$

$$\sqrt{v^2} = \sqrt{\frac{kx^2}{m}}$$

$$v = \sqrt{\frac{10000}{70}} = 12 \text{ m/s}$$

$0.580 = \frac{1}{2}mv^2$

# Student #13

ID#

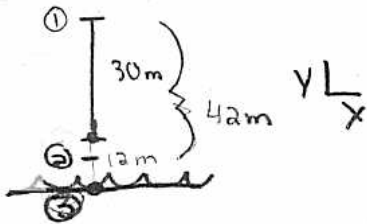
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- (b) Using the result of (a), find the dean's speed 7m above the water.



$$\begin{aligned} \text{a) } F_{\text{spring}} &= -kx \\ PE &= \frac{1}{2} kx^2 \end{aligned}$$

a) conservation of energy

$$\begin{aligned} \text{① } mgh &= \text{② } \frac{1}{2} kx^2 \\ (70 \text{ kg})(9.8 \text{ m/s}^2)(42 \text{ m}) &= \frac{1}{2} k(12 \text{ m})^2 \\ \underline{k} &= \underline{400.167} \end{aligned}$$

$$\begin{aligned} \text{b) } \text{② } \frac{1}{2} mv^2 + mgh + \frac{1}{2} k(5 \text{ m})^2 &= \text{① } mgh \\ \frac{1}{2} (70 \text{ kg})v^2 + (70 \text{ kg})(35 \text{ m})(9.8 \text{ m/s}^2) + \frac{1}{2} (400.167)(5 \text{ m})^2 &= \\ &= 70 \text{ kg}(42 \text{ m})(9.8 \text{ m/s}^2) \\ \frac{1}{2} (70 \text{ kg})v^2 &= 47819.9 \text{ J} \\ \underline{v} &= \underline{36.963 \text{ m/s}} \end{aligned}$$