

The University Student's 3 Rs

Reading, wRiting, and pRoblem solving

Using Context-Rich problems to facilitate learning



Ken Heller
School of Physics and Astronomy

Pat Heller
Department of Curriculum and Instruction

University of Minnesota

**15 year continuing project to improve undergraduate education with contributions by:
Many faculty and graduate students of U of M Physics & Education
In collaboration with U of M Physics Education Group**

Details at <http://groups.physics.umn.edu/physed/>

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A Guide for Discussion

✓ Goals for Instruction

Why Solve Problems?

What are Problems?

How are Problems Solved?

✓ Designing Problems

What is Context-Rich?

Why?

✓ Teaching Problem Solving?

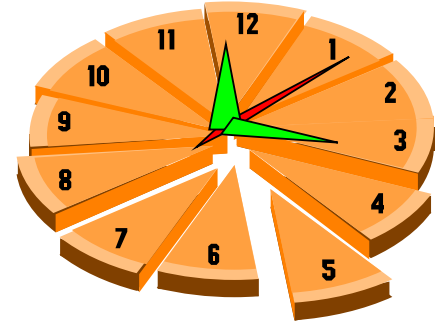
Possible Methods

Modeling a Framework

Supporting Real Problem Solving

Importance of Reading & Writing

✓ How Well Does It Work



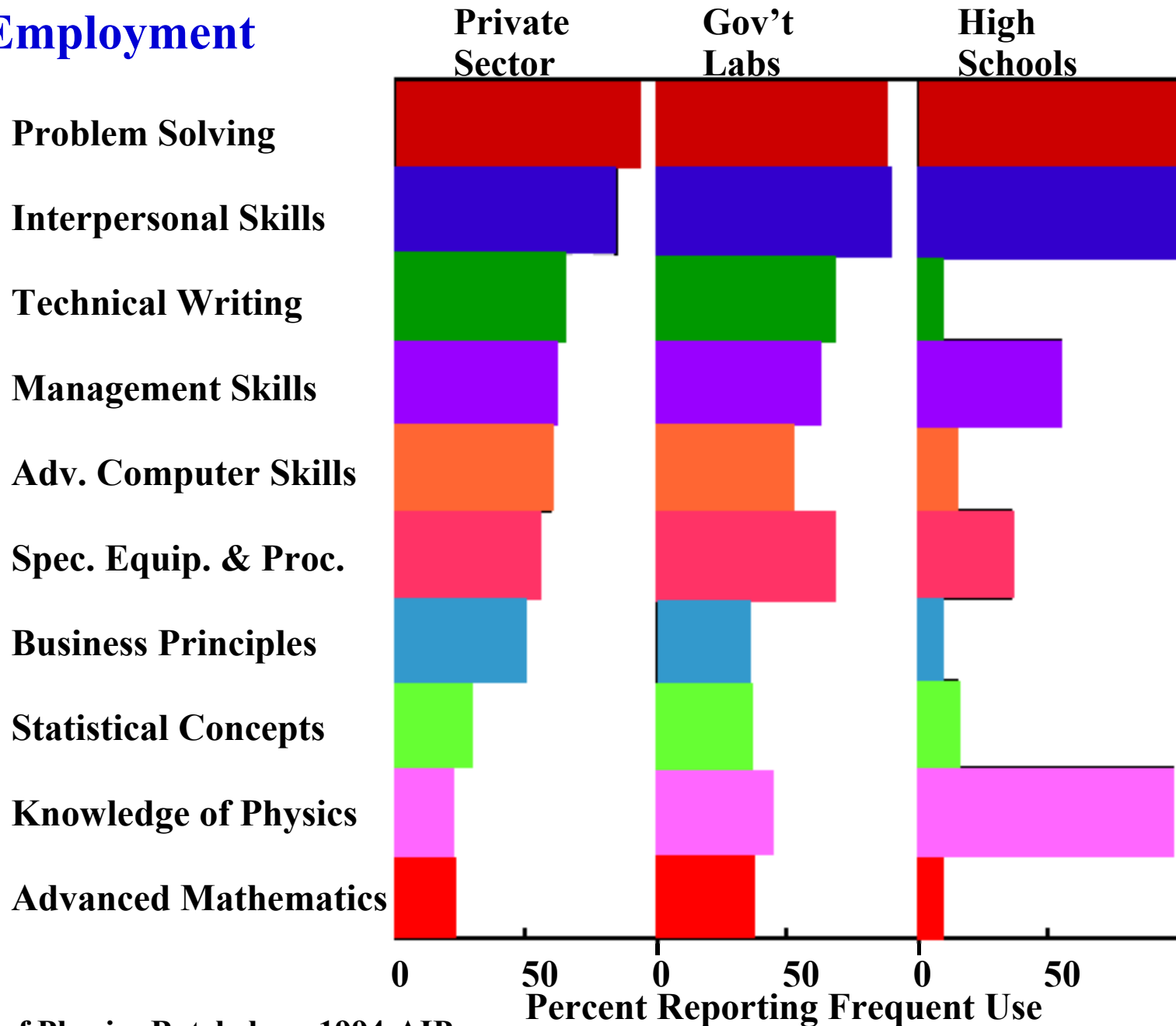
Why Teach Students to Solve Problems?

- ◆ **Society Wants It**
- ◆ **Industry Wants It**
- ◆ **Other Departments Want It**
- ◆ **Our Department Wants It**



What is IT?

Employment



Survey of Physics Bachelors, 1994-AIP

What Is Problem Solving?

“Process of Moving Toward a Goal When Path is Uncertain”

- If you know **how** to do it, its **not** a problem.



Problems are solved using tools



General-Purpose Heuristics

Not algorithms

“Problem Solving Involves **Error and Uncertainty**”



A problem for your student is not a problem for you



Exercise vs Problem



Some Heuristics



Means - Ends Analysis

identifying goals and subgoals

Working Backwards

step by step planning from desired result

Successive Approximations

range of applicability and evaluation

External Representations

pictures, diagrams, mathematics

General Principles of Physics

TASK

Discuss the types of problems you assign in your classes.
For your group list the common goals of these problems.

TIME ALLOTTED

5 minutes

PROCEDURES

Form a group of 3 people
Choose one person as a reporter

Formulate a response individually.

Discuss your response with your partners.

Listen to your partners' responses.

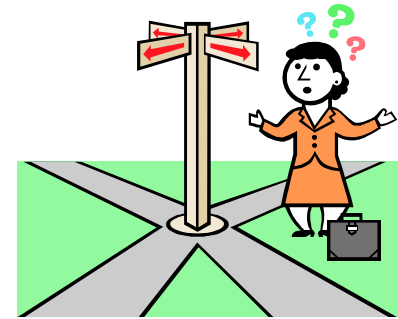
Create a new group response through discussion.



Solving Problems Requires Conceptual Knowledge:

From **Situations** to **Decisions**

- Visualize situation
- Determine goal
- Choose applicable principles
- Choose relevant information
- Construct a plan
- Arrive at an answer
- Evaluate the solution



Students must be taught *explicitly*

**The difficulty -- major misconceptions,
lack of metacognitive skills, no heuristics**

Problem Solving Requires

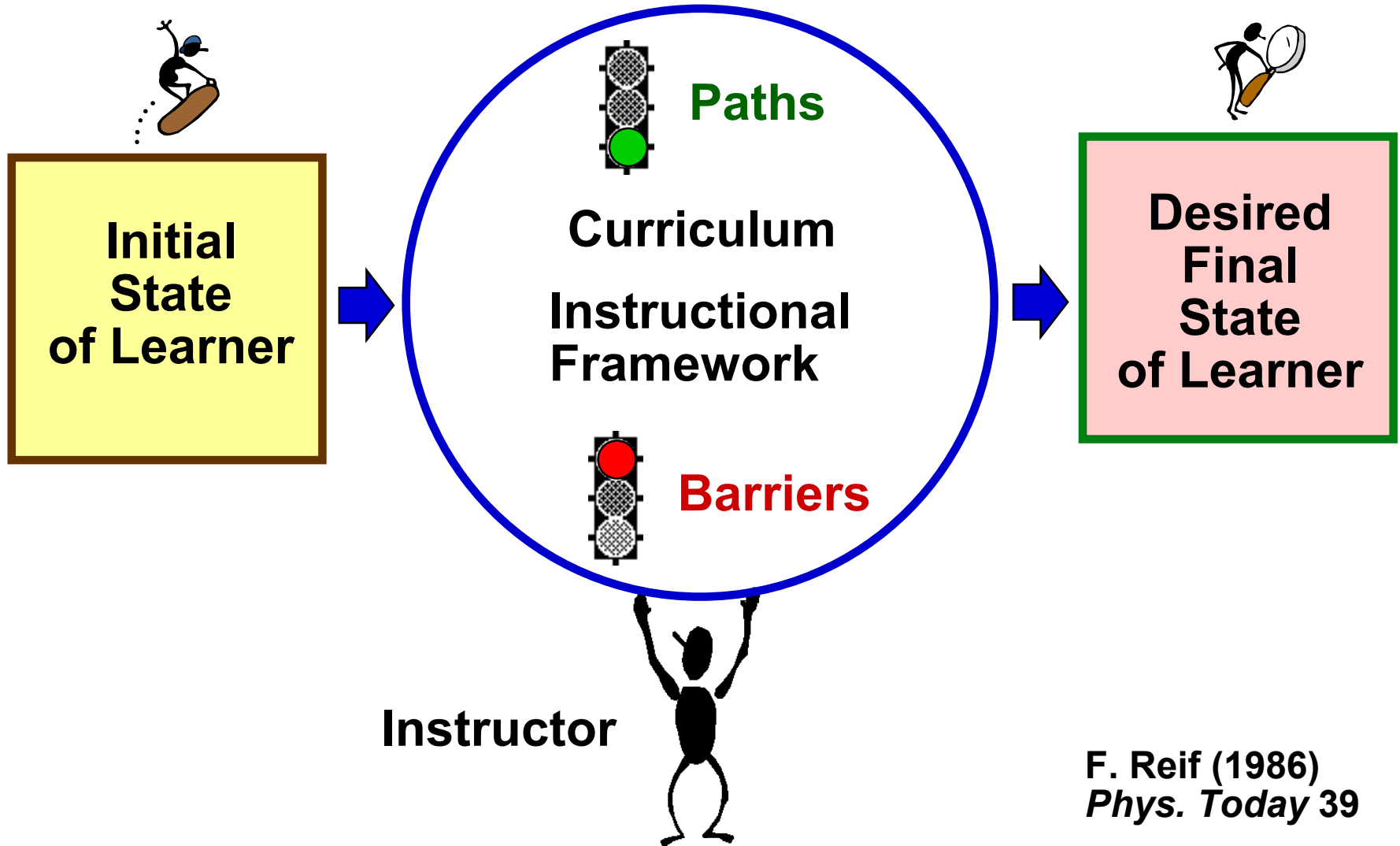
Metacognitive Skills

- **Managing time and direction**
- **Determining next step**
- **Monitoring understanding**
- **Asking skeptical questions**
- **Reflecting on own learning process**



Procedure for Change

Transformation Process



F. Reif (1986)
Phys. Today 39

Cognitive Apprenticeship Instruction

INSTRUCTION

Learning in the environment of expert practice



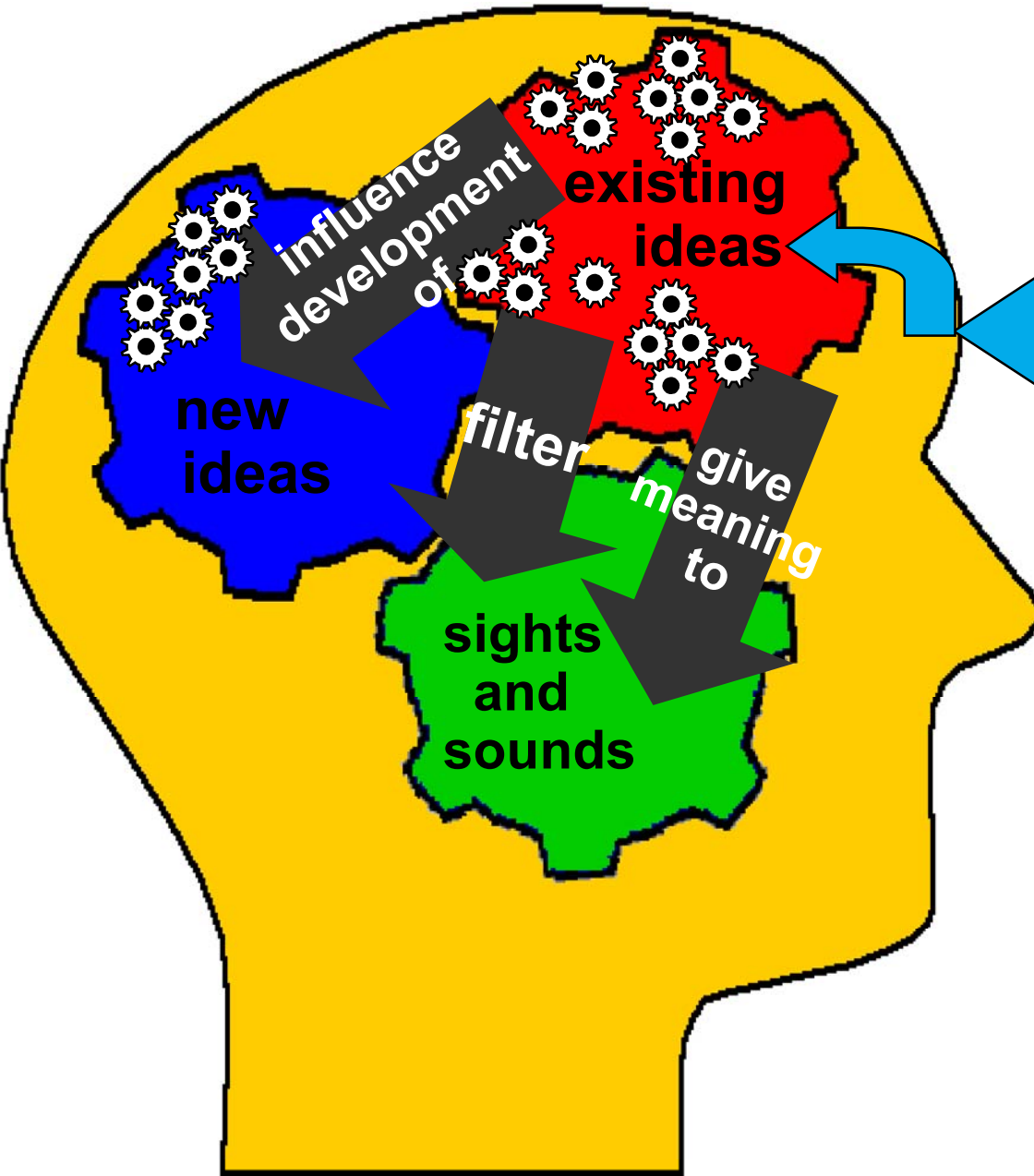
model



coach



fade



Collins, Brown, & Newman (1990)

Initial State of the Learner

Students have Misconceptions about

A Field of Knowledge

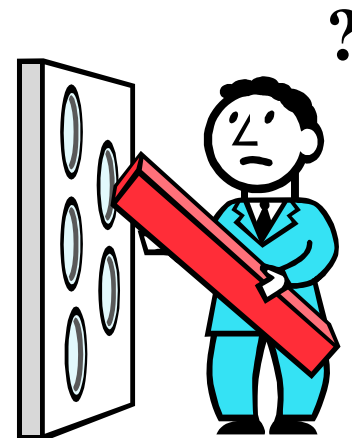
The Process of Learning

The Process of Problem-solving

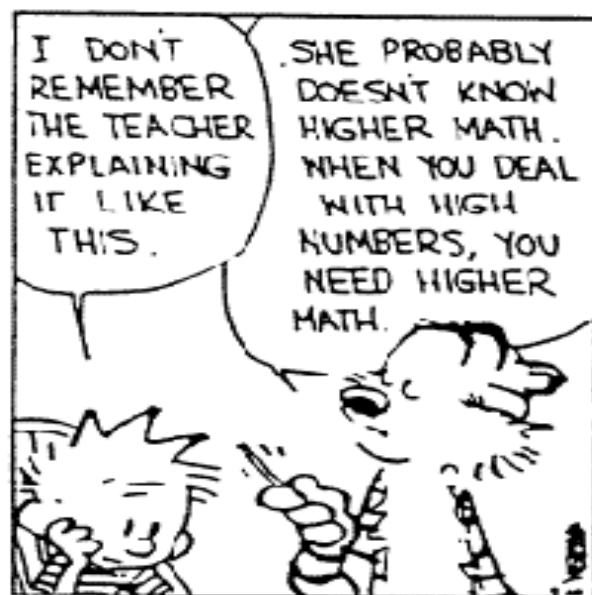
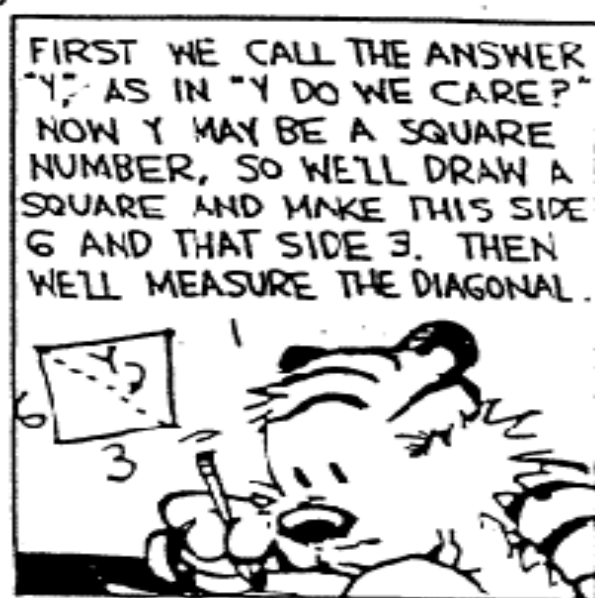
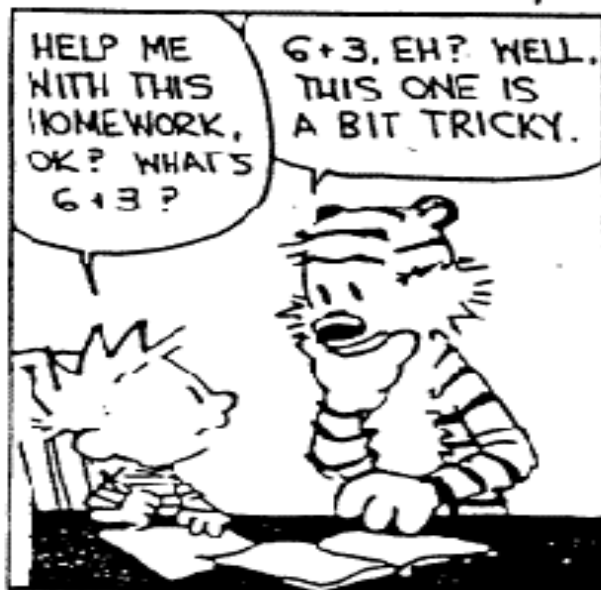
The Content of Your Field

All combine to make it difficult for students to solve problems.

Not the same as “getting a problem right”.



Calvin and Hobbes / By Bill Watterson



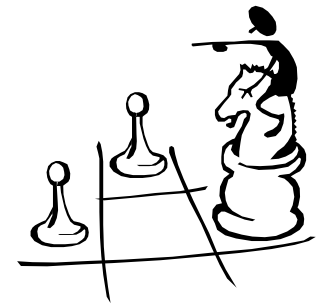
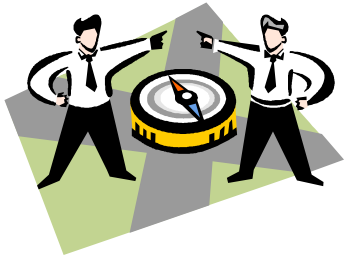
Appropriate Problems for Practicing Problem Solving

The problems must be challenging enough so there is a *real* advantage to using **problem solving heuristics**.

1. The problem must be **complex** enough so the best student in the class is not certain how to accomplish it.

The problem must be **simple** enough so that the solution, once arrived at, can be understood and appreciated.





2. The problems must be designed so that

- the major problem solving **heuristics** are **required** (e.g. a situation requiring an external representation);
- several **decisions** are **required** to make in order to accomplish the task (e.g. several ways to approach the problem);
- the problem **cannot be resolved in a few steps** by copying a pattern.





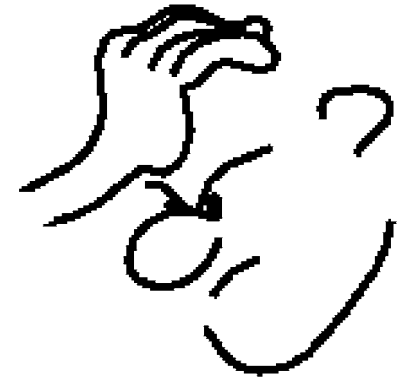
3. The task problem must connect to each student's mental processes

- the situation is **real** to the student so other information is connected;
- there is a **reasonable goal** on which to base decision making.



The Problem with Traditional Physics Problems

- ◆ Few decisions necessary
- ◆ Little visualization necessary
- ◆ Can usually be solved by manipulating equations
- ◆ Can often be solved without knowing physics
- ◆ Disconnected from student's reality



The Monotillation of Traxoline

(attributed to Judy Lanier)

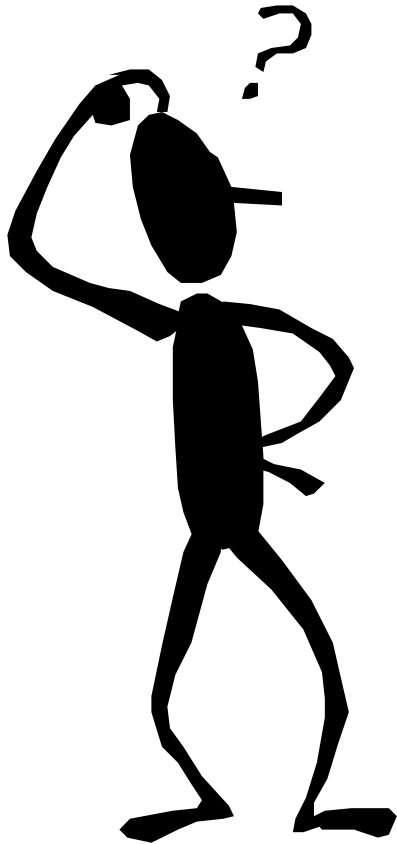
It is very important that you learn about traxoline. Traxoline is a new form of zionter. It is montilled in Ceristanna. The Ceristannians gristerlate large amounts of fevon and then brachter it to quasel traxoline. Traxoline may well be one of our most lukized snezlaus in the future because of our zionter lescedge.

Answer the following questions.

- 1. What is traxoline?**
- 2. Where is traxoline montilled?**
- 3. How is traxoline quasselled?**
- 4. Why is it important to know about traxoline?**

Do Students Practice Problem Solving?

A block starts from rest and accelerates for 3.0 seconds. It then goes 30 ft. in 5.0 seconds at a constant velocity.



- a. What was the final velocity of the block?
- b. What was the acceleration of the block?

Textbook Problem

Task

- ✓ Read at the following problem
- ✓ Discuss how you would go about solving it



TIME ALLOTTED - 10 minutes

***Discuss* your thoughts with your partners.**

***Create* a group response through discussion.**

Context-Rich Problem

You have a summer job with an insurance company and are helping to investigate a tragic "accident." At the scene, you see a road running straight down a hill that is at of 10° to the horizontal. At the bottom of the hill, the road widens into a small, level parking lot overlooking a cliff. The cliff has a vertical drop of 400 feet to the horizontal ground below where a car is wrecked 30 feet from the base of the cliff. A witness claims that the car was parked on the hill and began coasting down the road. He remembers that the car took about 3 seconds to get down the hill. Your boss drops a stone from the edge of the cliff and, from the sound of it hitting the ground below, determines that it takes 5.0 seconds to fall to the bottom. She tells you to calculate the car's average acceleration coming down the hill based on the statement of the witness and the other facts in the case. Obviously, she suspects foul play.

**Expert
"Real "Problem**

Acquire Problem

derived cues

**Understand problem (visualization).
Decide tentatively what principles to try.**

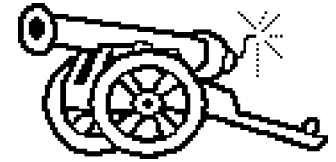
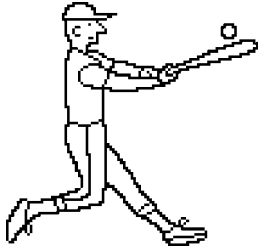
**Redescribe problem in terms of the field:
qualitative inferences, diagrams, and consideration of constraints
Categorize by possible approach**

**Plan: Start with an expression of principles, work *backwards*
from unknown.
Check -- enough information?**

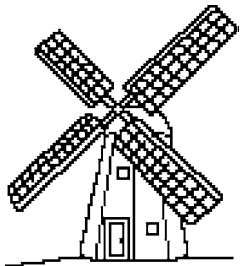
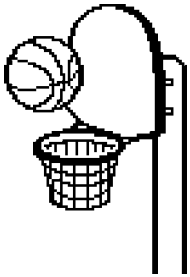
**Execute the plan
Check consistency**

Check/Evaluate answer

Context-rich Problems



- Each problem is a short story in which the major character is the student. That is, each problem statement uses the personal pronoun "**you.**"
- The problem statement includes a plausible **motivation** or reason for "you" to calculate something.
- The **objects** in the problems are **real** (or can be imagined) -- the idealization process occurs explicitly.
- **No pictures** or diagrams are given with the problems. Students must visualize the situation by using their own experiences.
- The problem can **not** be solved in **one step** by plugging numbers into a formula.



Because parents are concerned that children are taught incorrect science in cartoon shows, you have been hired as a technical advisor for the Cowboy Bob show. In this episode, Cowboy Bob is camped on the top of Table Rock. Table Rock has a flat horizontal top, vertical sides, and is 500 meters high. Cowboy Bob sees a band of outlaws at the base of Table Rock 100 meters from the side wall. The outlaws are waiting to rob the stagecoach. Cowboy Bob decides to roll a large boulder over the edge and onto the outlaws. Your boss asks you if it is possible to hit the outlaws with the boulder. Determine how fast Bob will have to roll the boulder to reach the outlaws.

2

Diagram: A boulder is launched from the top of a 500m high cliff. The initial velocity vector is at an angle of 11° below the horizontal. The horizontal distance to the outlaws is 100m. The acceleration is $g = 9.8 \text{ m/s}^2$.

Equations and calculations:

- $(5 = X)$
- $x = vt$
- $x = v_0 t + \frac{1}{2} a t^2$
- $300 =$
- $v = at$
- $x = at^2$
- $t = \frac{x}{v}$
- $t^2 = \frac{100m}{9.8 \text{ m/s}^2} = 11.3$
- $t = 3.36 \text{ s}$
- $t^2 = 51.0 \text{ s}$
- $t = 7.14 \text{ s}$
- $500^2 + 100^2 = \sqrt{260000} = 509.9 \text{ m}$
- $a = g = 9.8 \text{ m/s}^2$
- $x = x_0 + v_0 t + \frac{1}{2} a t^2$
- $x = x_0 + v_0 t + \frac{1}{2} a t^2$
- $\frac{1}{2} g t^2 = v_0 t \Rightarrow v_0 = \frac{0.5 g t^2}{t} = \frac{0.5 g t}{1}$
- $v_0 = 13.9 \text{ m/s}$
- $\tan \theta = \frac{v_{0y}}{v_{0x}} = \frac{7.14}{13.9}$
- $\theta = 26.6^\circ$
- $v_0 = 13.9 \text{ m/s}$
- $v_y = 71.4 \text{ m/s}$

he would have to roll the rock at 13.9 m/s

Students need instructional support to solve problems

Problem-solving Framework

Used by experts in all fields



STEP 1

Recognize the Problem

What's going on?

STEP 2

Describe the problem in terms of the field

What does this have to do with ?

STEP 3

Plan a solution

How do I get out of this?

STEP 4

Execute the plan

Let's get an answer

STEP 5

Evaluate the solution

Can this be true?

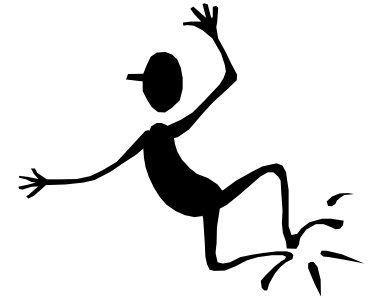
The Dilemma

Start with simple problems to learn expert-like strategy.



Success using novice strategy.

Why change?



Start with complex problems so novice strategy fails



Difficulty using new strategy.

Why change?



What Using Cooperative Groups Does for Teaching Problem Solving

1. Following a problem solving strategy seems too long and complex for most students.

Cooperative-group problem solving allows practice until the strategy becomes more natural.



2. Complex problems that need a strategy are initially difficult.

Groups can successfully solve them so students see the advantage of a logical problem-solving strategy early in the course.

What Using Cooperative Groups Does for Teaching Problem Solving

3. The group interactions externalize the planning and monitoring skills needed to solve problems allowing students to observe them. (Metacognition)
4. Students practice using the language of the field -- "talking physics."
5. Students must deal with and resolve their misconceptions.
6. Coaching by instructors is more effective



External clues of group difficulties
Group processing of instructor input

Cooperative Groups



- ◆ **Positive Interdependence**
- ◆ **Face-to-Face Interaction**
- ◆ **Individual Accountability**
- ◆ **Explicit Collaborative Skills**
- ◆ **Group Functioning Assessment**

Cooperative Group Problem Solving

Emphasis: Fundamental Physics Principles & Problem Solving

**Problem Design and Problem-solving Framework
based on expert-novice research**

Coaching based on collaborative learning research

Modify Lecture Style, Recitation and Laboratory

- **Lectures: MODEL** concept construction in problem context and competent problem solving
- **Recitation and Laboratory: COACH** problem solving

Scaffolding

- **Context-rich problems that require physics decisions**
- **Explicit problem-solving framework**
- **Structured cooperative groups**
- **Remove scaffolding: FADE** support



Student Problem Solutions

2

$t = \frac{d}{v}$

$(5 \times 10^3) = v \cdot t$

$x_{yf} = v_x t + \frac{1}{2} a t^2$

$x_{yf} = 300 = v_x t + \frac{1}{2} a t^2$

$v_x = v \cos \theta$

$v_x = v \cos 30^\circ$

$v_x = \frac{5000}{t}$

$\frac{5000}{t} = \frac{5000}{t} \cos 30^\circ + \frac{1}{2} (9.8 \text{ m/s}^2) t^2$

$\frac{5000}{t} (1 - \cos 30^\circ) = 4.9 t^2$

$5000 (1 - 0.866) = 4.9 t^2$

$5000 (0.134) = 4.9 t^2$

$670 = 4.9 t^2$

$t^2 = \frac{670}{4.9}$

$t^2 = 136.73$

$t = 11.69 \text{ s}$

$v_x = \frac{5000}{11.69} = 427.7 \text{ m/s}$

$v_y = v \sin \theta = 5000 \sin 30^\circ = 2500 \text{ m/s}$

$v = \sqrt{v_x^2 + v_y^2} = \sqrt{427.7^2 + 2500^2} = 2544.9 \text{ m/s}$

$\theta = \tan^{-1} \left(\frac{v_y}{v_x} \right) = \tan^{-1} \left(\frac{2500}{427.7} \right) = 80.1^\circ$

$x = v_x t + \frac{1}{2} a t^2 = 427.7 (11.69) + \frac{1}{2} (9.8) (11.69)^2 = 5000 \text{ m}$

$y = v_y t - \frac{1}{2} a t^2 = 2500 (11.69) - \frac{1}{2} (9.8) (11.69)^2 = 2500 \text{ m}$

$x = 5000 \text{ m}$

$y = 2500 \text{ m}$

$v_x = 427.7 \text{ m/s}$

$v_y = 2500 \text{ m/s}$

$v = 2544.9 \text{ m/s}$

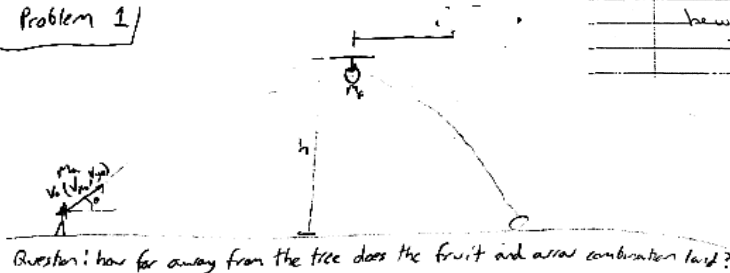
$\theta = 80.1^\circ$

we would have to roll the rock at 13.9 m/s

Initial State



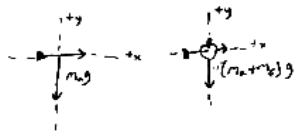
Problem 1



Question: how far away from the tree does the fruit and arrow combination land?

Approach: use conservation of momentum and kinematics
 assume constant acceleration due to gravity
 assume no momentum is lost in the collision
 neglect wind resistance
 use two intervals: from the time the arrow leaves the bow until just before it hits the fruit and just after it hits the fruit until they hit the ground
 the system is the earth and arrow for the first part, and the fruit and arrow combination and the earth for the second part.

Diagram



known: h, m_a, m_f, v_0, θ
 unknown: d

Qualitative relationships:

$$v_{x0} = v_0 \cos \theta \quad p_f = (m_a + m_f) v_{xf}$$

$$h = \frac{1}{2} g t^2 \Rightarrow \frac{2h}{g} = t^2, \sqrt{\frac{2h}{g}} = t$$

$$d = v_{xf} t$$

$$p_i = p_f \Rightarrow m_a v_{x0} = (m_a + m_f) v_{xf} \Rightarrow v_{xf} = \frac{m_a}{m_a + m_f} v_{x0}$$

$$p_i = m_a v_{x0}$$

Target: d

Plan the Solution:

unknown: d

$$d = v_{xf} t$$

v_{xf}, t

$$v_{xf} = \frac{m_a}{m_a + m_f} v_{x0}$$

v_{x0}

$$v_{x0} = v_0 \cos \theta$$

$$t = \sqrt{\frac{2h}{g}}$$

$$d = \frac{m_a}{m_a + m_f} v_0 \cos \theta \sqrt{\frac{2h}{g}}$$

Check units:

$$m = \frac{m_a}{m_a + m_f} \frac{m}{s} \sqrt{\frac{m}{m/s^2}} \rightarrow \sqrt{m^3/s^2}$$

$$m = \left(\frac{m}{s} \right) s$$

$$m = m \Rightarrow \text{OK}$$

is the answer complete?

yes, the distance was found in terms of the requested values

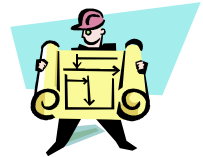
is the answer reasonable?

yes, the units check out OK and d will be smaller than h due to conservation of momentum

is the answer correctly stated?

yes, it is in units of distance, meters

Final State



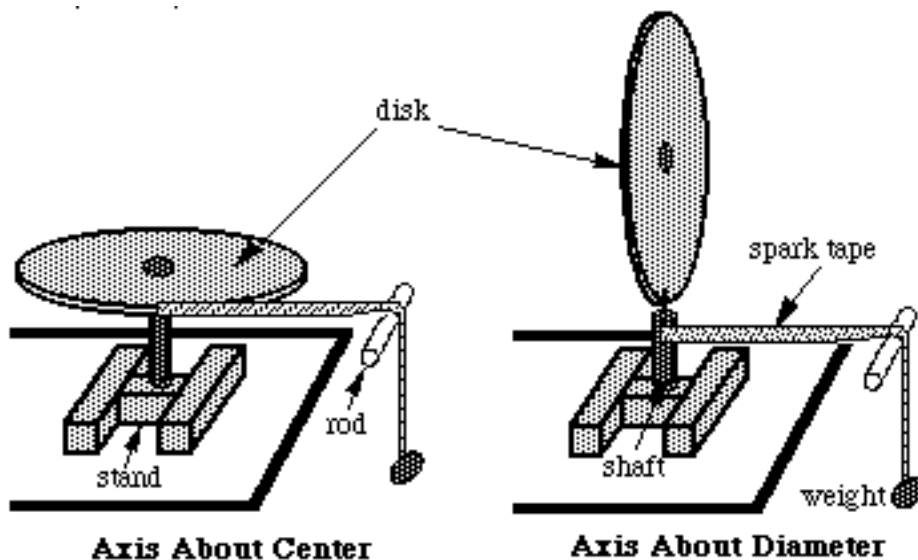
Importance of Laboratory Reports

- **Learning through synthesis of information**
 - Students write reports to **communicate** to **themselves** and their instructor their understanding of:
 - » Logical reasoning
 - » Physics concepts
 - » Data analysis choices
 - » What they've learned
 - » What they've not learned
- **Clear & Concise technical communication**
 - Necessary for upper level courses in all majors
 - Sought-after skills by employers
 - » **What is the decision**
 - » **Basis for the decision**
 - » **Consequences of the decision**



Problem Solving Laboratories

- **Closely integrated with lecture & recitation**
- **Always context-rich problems**
- **Emphasize modeling real systems**
- **Work in Cooperative Groups**
- **Lab reports are short technical memos**



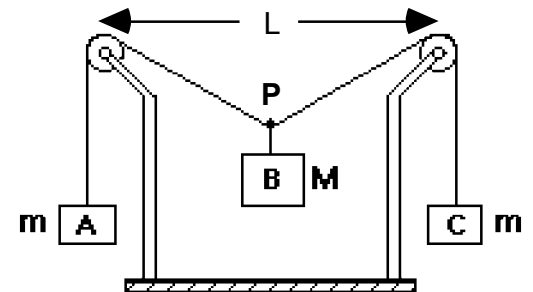
- **Each student hands in an individual laboratory report about every two weeks**
- **Each group member reports on a different problem**
- **TA assigns each student a problem at the end of each unit**
- **Student does not know which problem will be assigned.**
- **Report is due in 2 days.**

A Lab Problem:

Forces in Equilibrium

Mechanics Lab III, Problem #2

You have a summer job with a research group studying the ecology of a rain forest in South America. To avoid walking on the delicate rain forest floor, the team members walk along a rope walkway that the local inhabitants have strung from tree to tree through the forest canopy. Your supervisor is concerned about the maximum amount of equipment each team member should carry to safely walk from tree to tree. If the walkway sags too much, the team member could be in danger, not to mention possible damage to the rain forest floor. You are assigned to set the load standards. Each end of the rope supporting the walkway goes over a branch and then is attached to a large weight hanging down. **You need to determine how the sag of the walkway is related to the mass of a team member plus equipment when they are at the center of the walkway between two trees. To check your calculation, you decide to model the situation using the equipment shown.**



Guideline for grading laboratory reports

Problem Report:	Score
ORGANIZATION (clear and readable; correct grammar and spelling; section headings provided; physics stated correctly)	
DATA AND DATA TABLES (clear and readable; units and assigned uncertainties clearly stated)	
RESULTS (results clearly indicated; correct, logical, and well-organized calculations with uncertainties indicated; scales, labels and uncertainties on graphs; physics stated correctly)	
CONCLUSIONS (comparison to prediction & theory discussed with physics stated correctly ; possible sources of uncertainties identified; attention called to experimental problems)	

Given to TAs & Students in Lab Manual

General Criteria for evaluating technical Reports

(Dr. Lee-Ann K. Breuch, Dept. Of Rhetoric, U of MN)

What is the subject? What information needs to be included?

- **Content:** Is the information appropriate, accurate, and complete?
- **Context:** What is expected in the discipline for this type of document?
- **Audience:** To whom is the document written? How will it be used?
- **Organization:** How can the information be best organized? Can the information be divided into sections?
- **Support:** What details, facts, and evidence can be used to illustrate main points?

Example of quality levels - Content

	Satisfactory	Adequate	Poor
Addresses content accurately and thoroughly	Accurate and complete technical information, including equations, explanations, theory, and data.	Accurate technical information, but has missed some important information.	Does not include accurate or complete information.
Score	3	2	1

Example of quality levels - Support

	Satisfactory	Adequate	Poor
The paper has appropriate support for statements	Has necessary illustrations or figures. Refers to appropriate readings, theories, & relevant background information; includes relevant graphs & tables; with proper labeling & cross-references figures, tables, & graphs.	Has appropriate readings & background information, but does not use clear logic; has tables & graphs but they are not always labeled or cross-referenced.	Does not include necessary support in the form of logic, background information, tables, or graphs. No labeling, & cross-references.
Score	3	2	1

Example – Content & Support

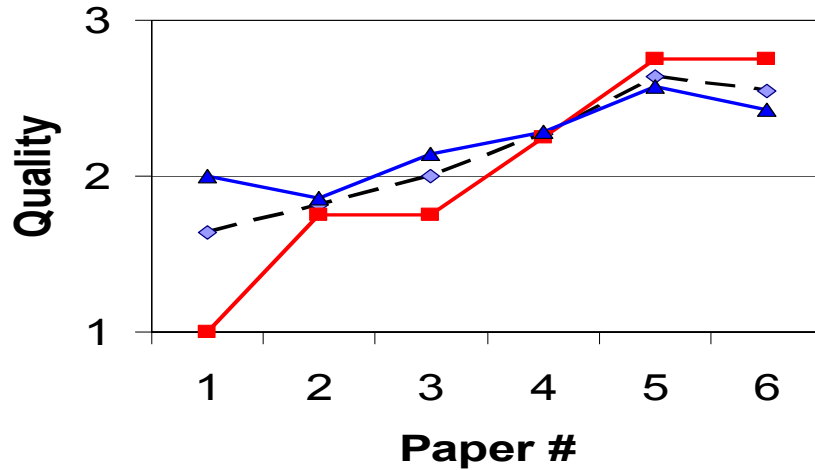
Satisfactory:

- While the beam was rotating we timed how long it took to make five revolutions. We did this to determine the angular velocity, ω . Once we knew ω we plugged that value into the equation $v = R\omega$, where R is the radius. Our group and I concluded that the linear velocity (v) of a point on the beam increases when the radius increases with a constant angular velocity. There is a graph at the end of the report that shows this relationship for easier understanding.

Adequate content & support:

- I observed that the acceleration is zero at the time where the cart switches from going up the track to down the track. This is what we predicted to happen. Our group ... The graph is a constant slope from left to right because the acceleration is always negative and this is why the graph is an upside down parabola. This lab has helped me understand ... The acceleration is always negative (in this respect) which is a little hard to comprehend at first but it was nice to observe this in lab.

Content



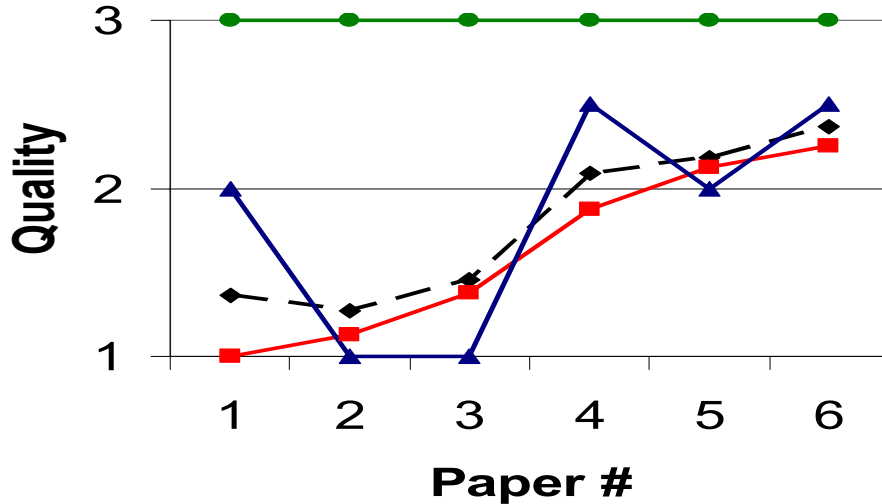
Class (11)
Poor (4)
Adequate (7)

Topic of paper
 number:

- 1) 1-D Kinematics**
- 2) 2-D Kinematics**
- 3) Forces**
- 4) Conservation of Energy and Momentum**
- 5) Rotational Kinematics**
- 6) Rotational Dynamics**

Content: What information needs to be included?

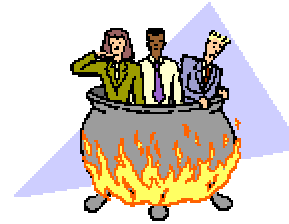
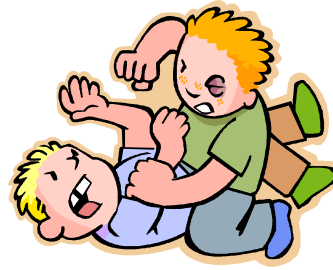
Support



Class (11)
Poor (8)
Adequate (2)
Satisfactory (1)

Support: What details, facts, and evidence are used?

Why Group Problem Solving May Not Work

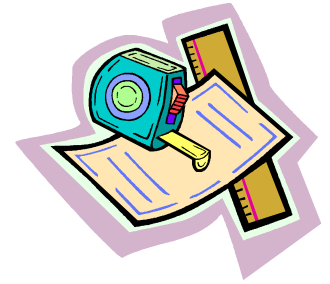
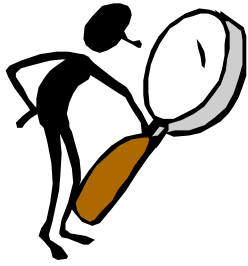


1. Inappropriate Tasks

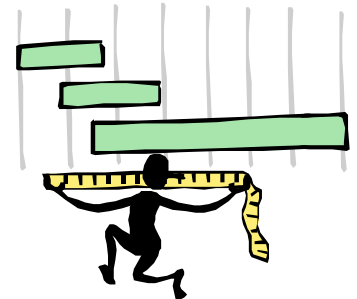
2. Inappropriate Grading

3. Poor structure and management of Groups

Data



- **Analysis of student exams**
- **Observation of student interactions**
- **Measures of conceptual understanding**
 - **FCI (Force Concept Inventory)**
 - **Other inventories**
 - **Open ended questions**
 - **Interviews**
- **Measures of hierarchical structure of physics**
- **Measures of student satisfaction**
 - **Surveys**
 - **Dropout rate**
- **Ease of implementation**



The End

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